

# Natural language syntax: parsing and complexity

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# Overview of the course

- Day 1: Formal languages and syntactic complexity.
- Day 2: The complexity of natural language.
- Day 3: Historic algorithms for parsing.
- Day 4: Modern approaches to parsing.
- Day 5: Neural networks and error propagation.









# Classifiers map states to actions

- **Classifier-based parser**: transition parser (e.g. Shift-Reduce) that relies on a classifier to select which action to apply).
- **Classifier**: function that maps each parsing state to an action.
- Sagae & Lavie 2005:
  - first occurrence of classifier-based constituency parsing;
  - variant of Shift-Reduce;
  - given a set of syntactic categories  $N$ , all  $\text{Reduce}(A \rightarrow BC)$ -s and all  $\text{Reduce}(A \rightarrow B)$ -s are available;
  - the input tokens are already tagged with POS tags from  $N$ ;
  - constraints on unary  $\text{Reduce}$ -s  $\rightarrow$  linear time complexity.

# From symbolic to statistical vectors

- Classifiers typically work on vector representations of the states.
- Past: states encoded as sparse vectors of symbolic features.  
Examples (for SR):
  - identity of the word on top of the stack,
  - distance in the sentence between the token on top of the stack and the first token in the buffer.
- Present: states encoded as dense vectors by neural networks.  
(→ Day 5)



# Classifier-based parsers are trained using treebanks

- Training requires data.
  - **Gold tree**: syntactic tree judged correct (e.g. obtained by expert annotation).
  - **Treebank**: set of gold trees.
  - Famously: the Penn Treebank (PTB; Marcus, Santorini & Marcinkiewicz 1993)
    - English text;
    - mainly from the news domain (WSJ);
    - ~50.000 sentences, ~1.000.000 tokens.
- Major impact on the statistical revolution in NLP.

# Training a parser with teacher forcing is simple

- Given a treebank, a simple training algorithm:

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**Algorithm 1:** Training of a transition parser (teacher forcing).

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```
Function train(dataset)
  classifier = init_classif();           // Initial (random) classifier.
  while ¬stop(classifier, dataset) do
    tree = dataset.get();
     $a_1, a_2, \dots, a_n$  = oracle(tree); // Seq. of actions that leads to the gold tree.
    state = init_state(tree);           // Initial parsing state.
    for  $i := 1$  to  $n$  do
      v = encode(state);                // Vector representation.
      classifier.optim(v,  $a_i$ );
      state = state.apply( $a_i$ );        // The "teacher" action is forced.
  return classifier;
```

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# Teacher forcing is suboptimal

- Depending on the *encode* function, training with teacher forcing might be super fast (due to parallelism).
- But this kind of training has defects, e.g. *error propagation*.
- Slower but better: not only strengthen a gold derivation, but also weaken the predicted one (as is done within the *structured perceptron* paradigm; Collins 2002).
- More on how to fight error propagation in Day 5.



# Classifier-based parsers can map any sequence to a tree

- Language recognised by a classifier-based parser: usually  $\Sigma^*$ .
- But the mapping from input (a sequence of tokens) to output (a tree) can be arbitrarily complex.
- What happens with ungrammatical sentences?

:/

- What happens with ambiguous sentences?

The most “natural” structure is predicted.

- → Classifiers encode a grammar with *preferences*.

# Quantifying the quality of constituent trees

- What matters: the quality of the analyses of grammatical sentences.

## Evaluating constituency parsing

$t_g$ : gold tree;  $t_p$ : predicted tree; both seen as sets of constituents

- **precision**:  $p = \frac{|t_g \cap t_p|}{|t_p|}$

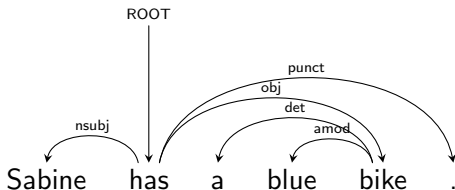
- **recall**:  $r = \frac{|t_g \cap t_p|}{|t_g|}$

- **F1**:  $\frac{2pr}{p+r}$

- SotA:  $> 0.96$  F1 on the PTB (e.g. Tian et al. 2020).

# Syntactic dependency tree

- First occurrence of classifier-based parsing: in the context of **dependency parsing** (Kudo & Matsumoto 2002)
- **Dependency**:
  - *governor*  $\xrightarrow{\text{label}}$  *dependent*
  - syntactic relationship between a token (gov.) and another (dep.) that it legitimates (allows or requires)



# A simple transition system for dependency parsing

- **Arc-Standard** (Nivre 2005, 2010):

- one of the simplest transition systems for (projective) dependency parsing;

- **shift:**

(stack, buffer, dependencies)  
 from state  $(S, w|B', A)$   
 to state  $(S|w, B', A)$

- **left-arc( $l$ ):**

(stack, buffer, dependencies)  
 from state  $(S'|w_l|w_r, B, A)$   
 to state  $(S'|w_r, B, A + w_l \xleftarrow{l} w_r)$

- **right-arc( $l$ ):**

(stack, buffer, dependencies)  
 from state  $(S'|w_l|w_r, B, A)$   
 to state  $(S'|w_l, B, A + w_l \xrightarrow{l} w_r)$



# Illustration of Arc-Standard

[ROOT] [Sabine has a blue bike .]





# Illustration of Arc-Standard

[ROOT Sabine] [has a blue bike .]

action: **shift**

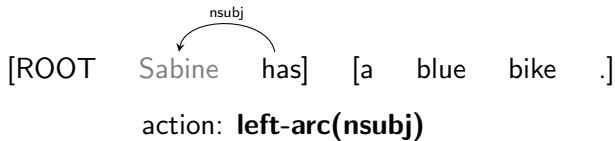


# Illustration of Arc-Standard

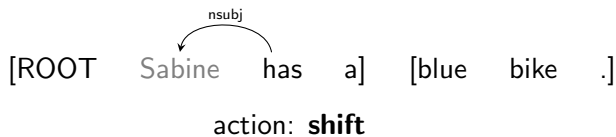
[ROOT Sabine has] [a blue bike .]

action: **shift**

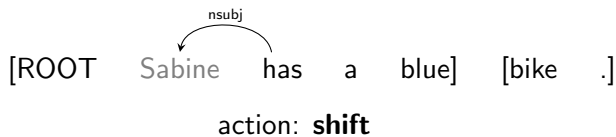
# Illustration of Arc-Standard



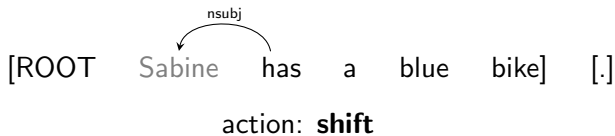
# Illustration of Arc-Standard



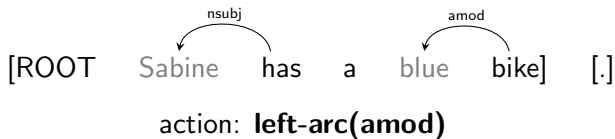
# Illustration of Arc-Standard



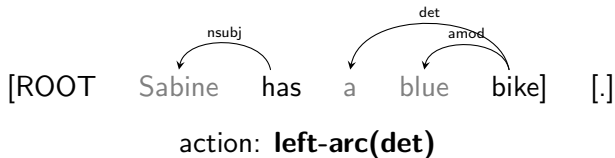
# Illustration of Arc-Standard



# Illustration of Arc-Standard

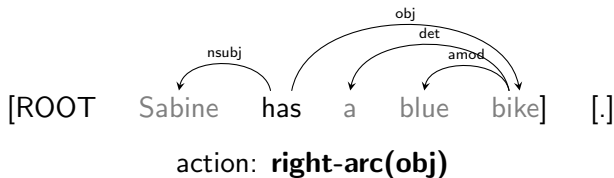


# Illustration of Arc-Standard

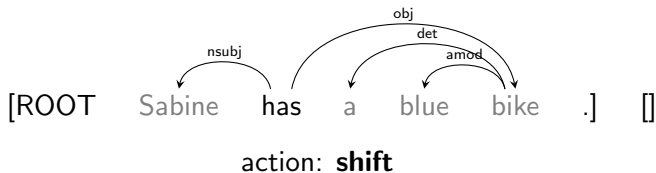




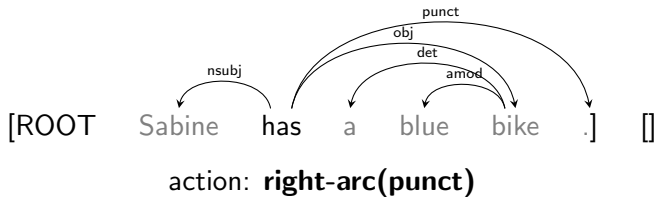
# Illustration of Arc-Standard



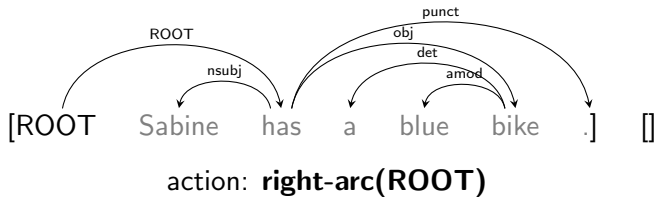
# Illustration of Arc-Standard



# Illustration of Arc-Standard



# Illustration of Arc-Standard



# Quantifying the quality of dependency trees

## Evaluating dependency parsing

$t_g$ : gold tree;  $t_p$ : predicted tree; both seen as sets of dependency  
(Standard practice: ignore punctuation; Chen & Manning 2014.)

- **labelled attachment score (LAS)**:  $\frac{|t_g \cap t_p|}{|t_g|}$
- **unlabelled attachment score (UAS)**: [similar but ignoring the dependency labels]
- SotA: > 0.96 LAS on a conversion of the PTB (e.g. Mrini et al. 2020).
- Universal Dependencies project (UD; Nivre et al. 2016, de Marneffe et al. 2021): treebanks for > 100 languages.  
<https://universaldependencies.org/>

# Another paradigm: graph-based parsing

- **Graph-based parsing:**
  - other paradigm for dependencies (McDonald et al. 2005),
  - requires a *scorer*,
  - simple incarnation:
    - ① score each candidate unlabelled dependency  $w_i \rightarrow w_j$ ;
    - ② compute  $\operatorname{argmax}_t \sum_{w_i \rightarrow w_j \in t} \operatorname{score}(w_i \rightarrow w_j)$  with the maximum spanning tree (MST) algorithm;
    - ③ label each dependency with a classifier.
- Scorer trained to assign higher scores to gold trees.
- Effective implementation: Dozat & Manning 2017.
- (Many variations are possible.)



# Scorers can be used in chart constituency parsing

- There are scorer-based versions of CYK.
- Gaddy, Stern & Klein 2018:
  - ① score each candidate constituent  $[X w_{i:j}]$ ;
  - ② compute  $\operatorname{argmax}_t \sum_{[X w_{i:j}] \in t} \operatorname{score}([X w_{i:j}])$  with a variant of CYK:
    - $\forall i, T[i, i + 1] = \max_X([X w_i])$
    - $\forall j > i + 1,$   

$$T[i, j] = \max_X([X w_{i:j}]) + \max_{i < k < j} (T[i, k] + T[k, j])$$
- Scorer trained to assign higher scores to gold trees.





# Supertagging is a very informative classification task

- **Supertagging:**

- for each token, predict a distribution of probability over all possible lexical categories (AKA **supertags**);
- classification task learned from an annotated corpus (e.g. CCGbank; Hockenmaier & Steedman 2007);

→  $\forall$  token  $w_i$ ,  $\forall$  supertag  $c$ ,  $P(C_i = c \mid w_{1:n})$ .

- Harder than POS tagging, but with accurate supertagging, parsing is “almost done”.

# A\* decoding for CCG (introduction)

- Lewis & Steedman (2014)'s decoding technique: bears some similarities with CYK and Earley, and also based on the *A\* search algorithm*.
- Two data structures:
  - **chart**,
    - collection of **partial analyses** (tree covering a span  $w_{i:j}$ ),
    - initially empty;
    - intuition: store for already done work;
  - **agenda**,
    - collection of partial analyses,
    - initialised as  $\{ \frac{w_i}{c} \mid \forall \text{ token } w_i, \text{ supertag } c \}$ ,
    - intuition: waiting queue for remaining work.

# A\* decoding for CCG (scores)

- **Score** of an analysis of  $w_{i:j}$ : product of two values defined based on the supertags used for  $w_{i:j}$ ,

- **internal score**,

$$\prod_{k=i}^j P(C_k = c_k \mid w_{1:n});$$

- **external score**,

$$\prod_{k=1}^{i-1} \max_c P(C_k = c \mid w_{1:n}) \times \prod_{k=j+1}^n \max_c P(C_k = c \mid w_{1:n}).$$

- The score of an analysis is an upper bound of the score of any of its *extensions* (because the  $\max$ ·s are replaced by equal or lower probabilities).

# A\* decoding for CCG (overview)

- ① Take the highest scoring partial analysis out of the agenda.
  - ② If this analysis covers the whole sentence, parsing is over: output this analysis.
  - ③ Otherwise:
    - add this analysis to the chart,
    - add to the agenda all possible analyses obtained from it using any syntactic rule, combining it with other partial analyses found *in the chart* (and not in the agenda).
  - ④ Go back to step 1.
- exact search (the output is the highest scoring analysis)

# A\* decoding for CCG (example)

- Simplified example on “Sabine likes books”, forward/backward applications and three supertags only.

- Supertagging:

- $P(c_1 = N \mid w_{1:4}) = 0.15$ ,  $P(c_1 = NP \mid w_{1:4}) = 0.8$ ,  $P(c_1 = (S \setminus NP)/NP \mid w_{1:4}) = 0.05$

- $P(c_2 = N \mid w_{1:4}) = 0.05$ ,  $P(c_2 = NP \mid w_{1:4}) = 0.05$ ,  $P(c_2 = (S \setminus NP)/NP \mid w_{1:4}) = 0.9$

- $P(c_3 = N \mid w_{1:4}) = 0.5$ ,  $P(c_3 = NP \mid w_{1:4}) = 0.45$ ,  $P(c_3 = (S \setminus NP)/NP \mid w_{1:4}) = 0.05$

- Initial chart:  $\square$

- Initial agenda:  $\left[ \begin{array}{c} \text{likes}_2 \\ \hline (S \setminus NP)/NP \end{array} \quad (0.9 \times 0.4), \quad \begin{array}{c} \text{Sabine}_1 \\ \hline NP \end{array} \quad (0.8 \times 0.45), \right.$   
 $\left. \begin{array}{c} \text{books}_3 \\ \hline N \end{array} \quad (0.5 \times 0.72), \quad \begin{array}{c} \text{books}_3 \\ \hline NP \end{array} \quad (0.45 \times 0.72), \quad \begin{array}{c} \text{Sabine}_1 \\ \hline N \end{array} \quad (0.15 \times 0.45), \dots \right]$

# A\* decoding for CCG (example)

- Chart: [  $\frac{\text{likes}_2}{(S \setminus NP)/NP}$  ]
- Agenda: [  $\frac{\text{Sabine}_1}{NP}$  (0.8 × 0.45) ,  $\frac{\text{books}_3}{N}$  (0.5 × 0.72) ,  $\frac{\text{books}_3}{NP}$  (0.45 × 0.72) ,  $\frac{\text{Sabine}_1}{N}$  (0.15 × 0.45) , ... ]



# A\* decoding for CCG (example)

- Chart: [  $\frac{\text{likes}_2}{(S \setminus NP)/NP}$  ,  $\frac{\text{Sabine}_1}{NP}$  ]
- Agenda: [  $\frac{\text{books}_3}{N}$   $(0.15 \times 0.45)$  ,  $\frac{\text{books}_3}{NP}$   $(0.45 \times 0.72)$  ,  $\frac{\text{Sabine}_1}{N}$   $(0.5 \times 0.72)$  , ... ]



# A\* decoding for CCG (example)

- Chart: [  $\frac{\text{likes}_2}{(S \setminus NP)/NP}$  ,  $\frac{\text{Sabine}_1}{NP}$  ,  $\frac{\text{books}_3}{N}$  ]
- Agenda: [  $\frac{\text{books}_3}{NP}$   $(0.45 \times 0.72)$  ,  $\frac{\text{Sabine}_1}{N}$   $(0.15 \times 0.45)$  , ... ]





# A\* decoding for CCG (example)

- Chart: [  $\frac{\text{likes}_2}{(S \setminus NP) / NP}$  ,  $\frac{\text{Sabine}_1}{NP}$  ,  $\frac{\text{books}_3}{N}$  ,  $\frac{\text{books}_3}{NP}$  ]
- Agenda: [  $\frac{\frac{\text{likes}_2}{(S \setminus NP) / NP} \frac{\text{books}_3}{NP}}{S \setminus NP} \xrightarrow{(0.405 \times 0.8)}$  ,  $\frac{\text{Sabine}_1}{N} \xrightarrow{(0.15 \times 0.45)}$  , ... ]

## A\* decoding for CCG (example)

- Chart: [  $\frac{\text{likes}_2}{(S \setminus NP) / NP}$  ,  $\frac{\text{Sabine}_1}{NP}$  ,  $\frac{\text{books}_3}{N}$  ,  $\frac{\text{books}_3}{NP}$  ,  
 $\frac{\text{likes}_2 \text{ books}_3}{(S \setminus NP) / NP \quad NP}$  ]  
 $\frac{\text{likes}_2 \text{ books}_3}{(S \setminus NP) / NP \quad NP} \xrightarrow{\quad} S \setminus NP$
- Agenda: [  $\frac{\text{Sabine}_1}{NP}$   $\frac{\text{likes}_2 \text{ books}_3}{(S \setminus NP) / NP \quad NP}$   $(0.324 \times 1)$  ,  $\frac{\text{Sabine}_1}{N}$   
 $\frac{\text{likes}_2 \text{ books}_3}{(S \setminus NP) / NP \quad NP} \xrightarrow{\quad} S \setminus NP$   
 $\frac{\text{likes}_2 \text{ books}_3}{(S \setminus NP) / NP \quad NP} \xrightarrow{\quad} S$   
 $(0.15 \times 0.45) , \dots ]$



# A\* decoding for CCG (example)

- Chart: [  $\frac{\text{likes}_2}{(S \setminus NP) / NP}$  ,  $\frac{\text{Sabine}_1}{NP}$  ,  $\frac{\text{books}_3}{N}$  ,  $\frac{\text{books}_3}{NP}$  ,   
 $\frac{\text{likes}_2 \text{ books}_3}{(S \setminus NP) / NP \quad NP}$  ]   
 $\frac{\quad}{S \setminus NP} >$
- Agenda: [  $\frac{\text{Sabine}_1}{N} (0.15 \times 0.45) , \dots ]$
- Output:  $\frac{\text{Sabine}_1 \quad \text{likes}_2 \quad \text{books}_3}{NP \quad (S \setminus NP) / NP \quad NP}$    
 $\frac{\quad}{S \setminus NP} >$    
 $\frac{\quad}{S} <$

# CCG parsing is useful

- CCG parsing for English works in practice.
- Intuition: There is a nice balance between the number of supertags ( $\sim 400$ ) and the number of syntactic rules ( $\sim 20$ ).
- CCG comes with a compositional syntax-semantics interface.
- $\rightarrow$  CCG powers state-of-the-art symbolic natural language inference (NLI) systems (e.g. Haruta, Mineshima & Bekki 2022).



## Day 4: Summary

- An ML component (classifier/scorer) can replace a grammar.
- This is possible both in transition and chart parsing.
- Doing so requires data (usually treebanks).
- Dependency parsing is popular; either transition- or graph-based.
- For CCG and TAG: the supertagging+decoding paradigm combines a classifier and a grammar.
- Grammar-based parsing can be convenient for compositional semantics.



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